Askesis: Introduction

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1 Perceptron model of a neuron

A perceptron has two possible outputs, 1 (representing firing) and 0 (representing not firing). Let its inputs be denoted by $x_1, \ldots, x_n$. The rule is then

$$y = \begin{cases} 1 & \sum_i w_i x_i > \theta \\ -1 & \text{otherwise} \end{cases}$$

The x_i can usually be taken to be either 0 (if the input neuron fires) or 1 (if the input neuron does not fire). Neurons that do not fire are thus not included in the sum. Occasionally, it is helpful to think about x_i between zero and one, in which case it can be encoded by the firing rate. So, if the neuron fires at its maximum rate, that is represented by a one, and if it doesn't fire at all, that is represented by a zero. If it fires at a tenth its firing rate, that is represented by 0.1.

The w_i are called the synapse weights; each is a summary of properties of the synapse that occurs between the i-th input neuron and the output neuron. These properties include the physical distance between the two neurons, as well as the concentration of neurotransmitter receptors in the output neuron, and other things as well. If $w_i > 0$, then we call the synapse "excitatory" - the firing of the input neuron excites the output neuron. Most excitatory synapses use the neurotransmitter glutamate. If $w_i < 0$, we call the synapse "inhibitory" - the firing of the input neuron inhibits the output neuron. Most inhibitory synapses use the neurotransmitter GABA (Gamma-Aminobutyric acid). In actual neurons, a single neuron releases a single main neurotransmitter, and is therefore only ever excitatory (all synapses it outputs to are excitatory) or inhibitory (all synapses it outputs to are inhibitory). The parameter θ controls how excitable the neuron is, and can be modified by learning. This is called "intrinsic plasticity".

A perceptron is much simpler than a neuron, but is a reasonable first-pass approximation. Our model does not require anything more complicated than perceptrons.

The word "perceptron" actually refers to two things: the model above, and a learning algorithm. We will describe the learning algorithm here. First, we

I like to think of glutamate as the "black ink" and GABA as the "red ink" of the nervous system.

add an x_0 that is always 1, and let $w_0 = -\theta$. The perceptron then fires if $\sum_{i=0}^{n} w_i x_i > 0$. We then suppose that we see a sequence of inputs $x_i(t)$, each labeled either 1 or -1 by a desired output $\widehat{y}(t)$. The learning rule is then as follows: if the output y of the neuron was the same as $\widehat{y}(t)$, we do nothing. If $y(t) \neq \widehat{y}(t)$, then we update the weights as follows:

$$w_i(t+1) = w_i(t) + \alpha(\widehat{y}(t) - y(t))x_i.$$

The parameter α is called the learning rate; high values of α result in a system that changes its parameters more quickly and thus learns more quickly. A lower learning rate can be desirable, since the system will be less likely to lose the information it already has.

2 Basic overview of the cerebellum

3 Cell types

The cerebellum contains a number of different types of cells:

Mossy fiber Mossy fibers are the axons of neurons outside of the cerebellum. They constitute one of the two sources of input of the cerebellum. One of the major sources of mossy fibers is the pontine nuclei, which relay information from the cerebrum.

All mossy fibers are excitatory. The mossy fibers excite granular cells and Golgi cells, and collaterals (side branches) of the mossy fibers excite deep nuclear cells.

Mossy fibers participate in both the positive and negative pathways.

Deep nuclear cell These are the main source of output from the cerebellum. (Some Purkinje cells project to the vestibular nuclei, which seem to be pretty similar to the deep nuclei.)

Some of the deep nuclei are: interposed nucleus, fastigial nucleus, dentate nucleus.

There are two kinds of deep nuclear cell, large and small. The large cells can be excitatory or inhibitory, and project to premotor areas. The small cells are inhibitory and project to the inferior olive.

Deep nuclear cells receive input from mossy fiber collaterals, climbing fiber collaterals, and Purkinje cells.

Deep nuclear cells participate in both the positive and negative pathways.

Inferior olive cell These are the second source of input to the cerebellum. They receive an "efference" copy of the signals sent from the cerebrum to the spinal cord.

The inferior olive cells are excitatory and send climbing fibers into the cerebellum to make contact with the Purkinje cells, stellate cells, and
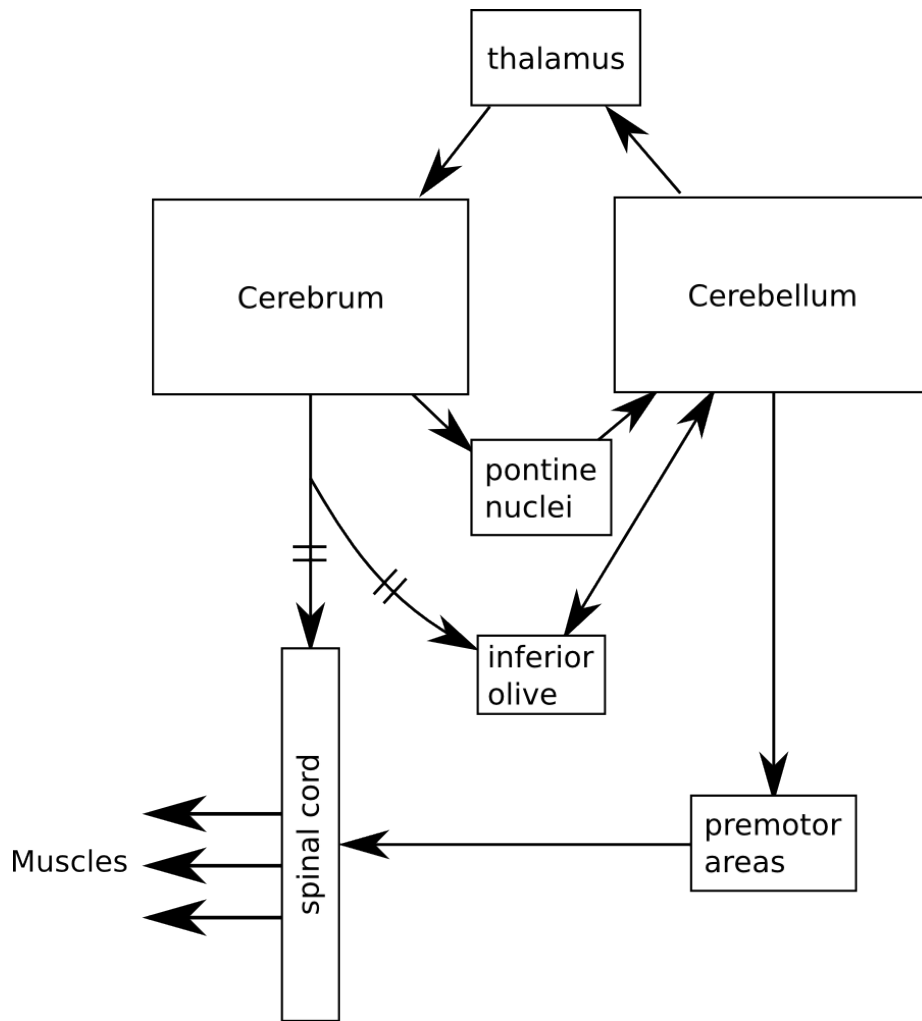
Figure 1: Inputs and outputs of the cerebellum. The two arrows marked with double lines represent two neural pathways that convey copies of the same information.
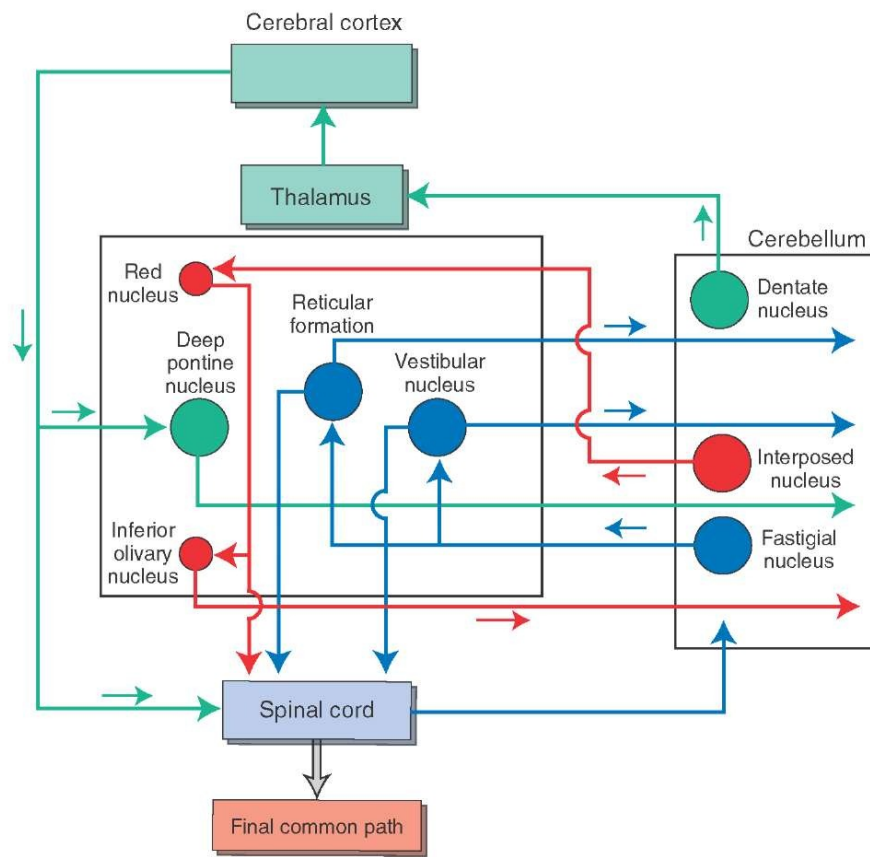
Figure 2: How the cerebellum fits into the rest of the brain. Courtesy of http://what-when-how.com/wp-content/uploads/2012/04/tmp15F121.jpg
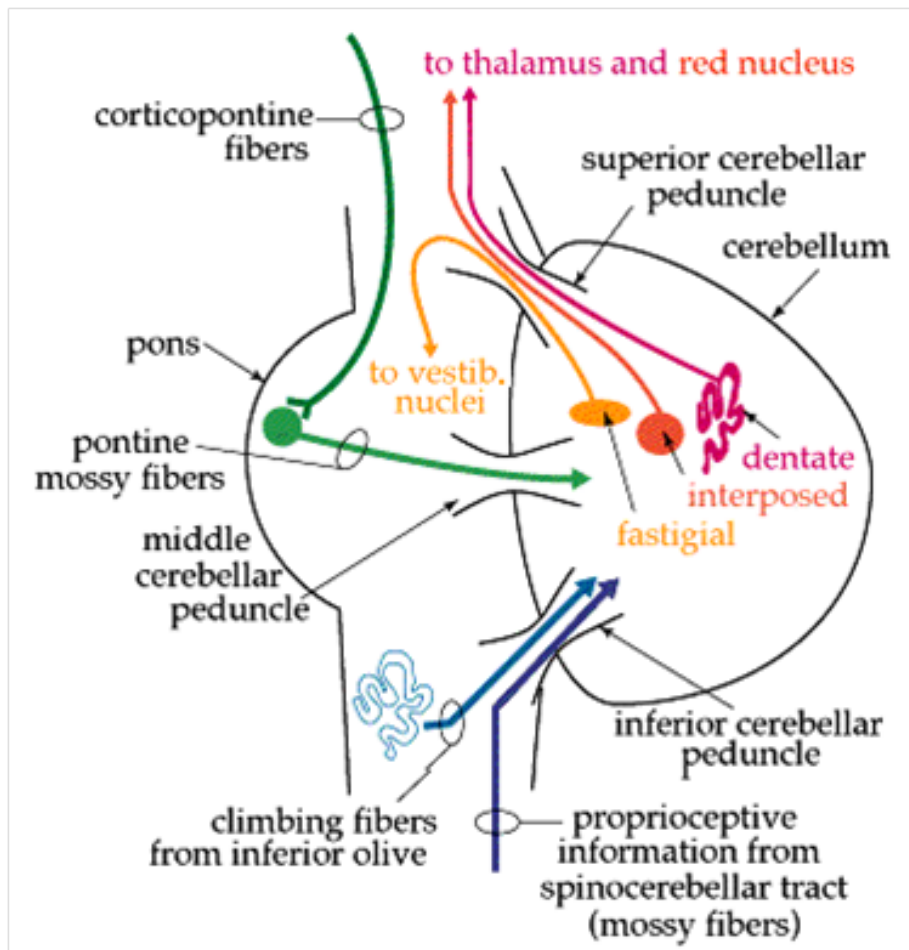
Figure 3: Pathways into and out of the cerebellum. The fastigial, interposed, and dentate nuclei (and some others) are collectively referred to as the deep nuclei, as they lie deep within the cerebellum. Courtesy of http://www.dizziness-and-balance.com/anatomy/brain/cerebellum.htm

basket cells. A single climbing fiber impulse will cause a Purkinje cell to fire.

Collaterals of the climbing fiber make contact with the deep nuclear cells.

Inferior olive cells participate in both the positve and negative pathways.

Purkinje cell The Purkinje cells are inhibitory, and send their output to the deep nuclear cells. They receive input mainly from the parallel fibers, which are the output of the granular cells. They also receive some input directly from nearby granular cells.

Purkinje cells fire at a certain base rate even when not receiving any input.

Purkinje cells participate in the negative pathway.

Basket/stellate cell Basket and stellate cells inhibit the Purkinje cells (and thus disinhibit the deep nuclear cells by proxy).

The stellate cells occupy the outermost portions of the cerebellar cortex, while basket cells are slightly more inward. There is also an intermediate type of cell that occurs between the basket cells and stellate cells and has an appearance halfway between the two.

Basket and stellate cells participate in the negative pathway.

Granular cell Granular cells receive input from 4-5 mossy fibers. Granular cells are excitatory. The output of the granular cell is the parallel fiber, which sends input to the Purkinje cells, basket cells, and stellate cells.

Granular cells are generally thought to fire only when multiple of their inputs are active.

Granular cells are the most numerous neurons in the brain; about three-fourths of the neurons in the brain are granular cells in the cerebellum. (Granular cells are very small, so the cerebellum only takes up about 10% of the volume of the brain.)

Granular cells participate in the negative pathway.

4   Learning

As a brief aside to anyone not versed in machine learning or neuroscience, "learning" is a term that describes changing the structure or parameters of a system in order to make that system better achieve some goal or perform some purpose correctly. The best understood mechanism for learning in the brain is changing the strength of synapses, the gaps between two neurons, usually by changing the number of receptors that respond to neurotransmitters.

unsure whether we actually want this paragraph - does it make us sound like a noob?
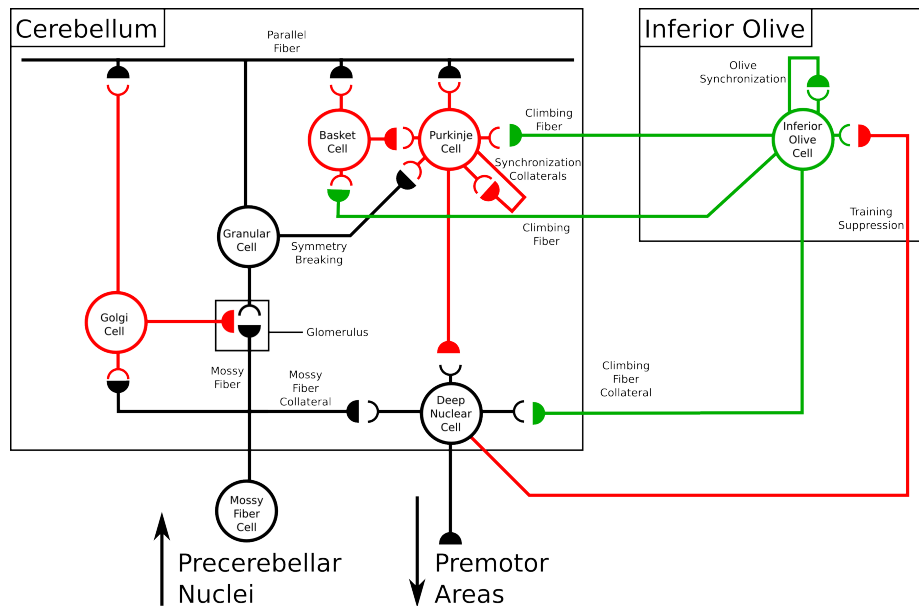
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Figure 4: Cells of the cerebellum. Excitatory cells are shown in black, while inhibitory cells are shown in red. Inputs to a cell are shown as an empty half circle, while outputs are shown as a full half circle. Cells of the inferior olive are shown in green, to emphasize that their output is used to train the targeted cells; they are excitatory. There are two kinds of deep nuclear cell: one excitatory and projecting either back into the cerebellum or to premotor areas; and one inhibitory and projecting to the inferior olive. Since the cells receive the same input, we have simplified the picture by identifying them together.

Figure 14.13 Schematic diagram of the Purkinje cell and its connections with neurons of other types in the cerebellum (Part 1)
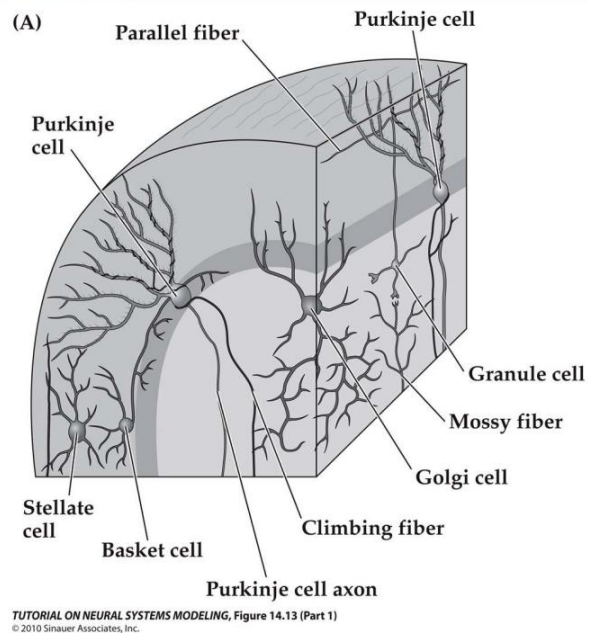
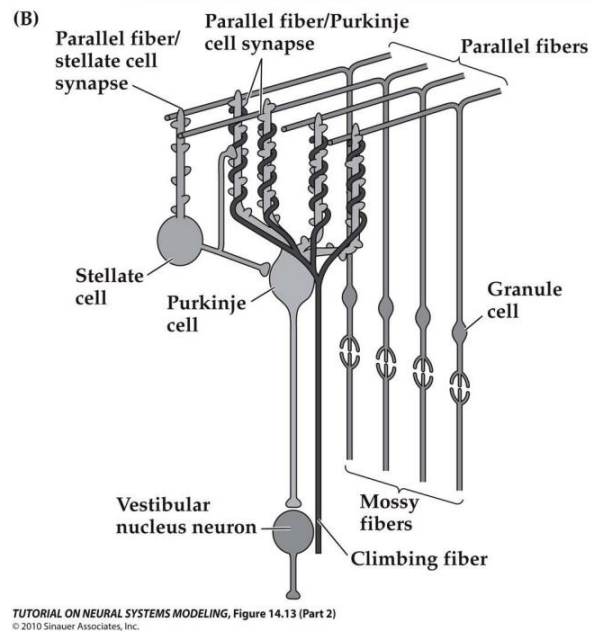Figure 5: Cells of the cerebellum. Courtesy of https://nanohub.org/resources/18948/watch?resid=19060

Figure 14.13 Schematic diagram of the Purkinje cell and its connections with neurons of other types in the cerebellum (Part 2)

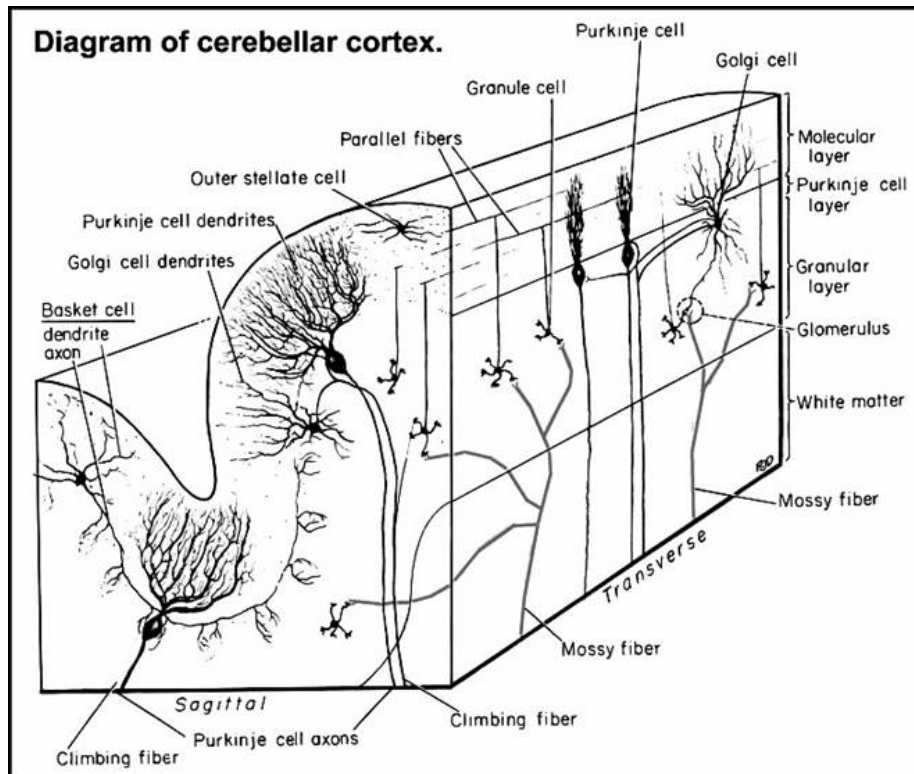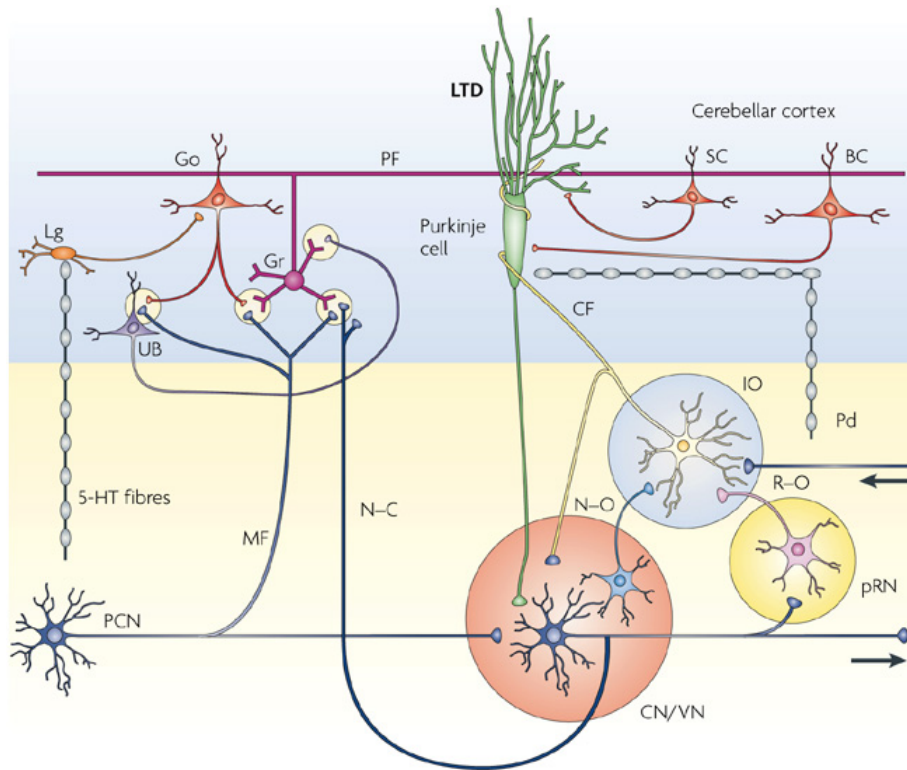Figure 6: Cells of the cerebellum. Courtesy of https://nanohub.org/resources/18948/watch?resid=19060

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Figure 7: Cells of the cerebellum. Courtesy of http://www.scritub.com/limba/engleza/health/CEREBELLUM25854.php

Figure 8: Cells of the cerebellum. Courtesy of http://www.nature.com/nrn/journal/v9/n4/images/nrn2332-f3.jpg.
PCN:pontine nuclei. MF: mossy fiber. Lg: Lugaro cell. 5-HT fibres: beaded fibers. UB: unipolar brush cells (found only in the vestibulocerebellum). Go: Golgi cell. Gr: Granular cell. N-C: state cell pathway. CN/VN: deep nuclei and vestibular nuclei. PF: parallel fiber. LTD: long-term depression, the learning mechanism of the Purkinje cell. SC: stellate cell. BC: basket cell. CF: climbing fiber. N-O: training suppression cell pathway to inferior olive. IO: inferior olive. R-O: red nucleus to inferior olive pathway. pRN: parvocellular (small cells) red nucleus.